## **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**International General Certificate of Secondary Education** 

## MARK SCHEME for the October/November 2013 series

## 0580 MATHEMATICS

0580/43

Paper 4 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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## **Abbreviations**

cao correct answer only cso correct solution only

dep dependent

ft follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

www without wrong working art anything rounding to soi seen or implied

Qu.	Answers	Mark	Part Marks
1 (a) (i)	45	2	M1 for $5 \times 63 \div 7$
(ii)	20	2	<b>M1</b> for $5 \times 56 \div 14$
(iii)	23.4 or 23.38 to 23.41	3	<b>M2</b> for $\frac{13 \times 4.9 - 48.8}{13 \times 4.9} \times 100$
			or $\frac{4.9 - 48.8 \div 13}{4.9} \times 100$ Or
			M1 for $\frac{13 \times 4.9 - 48.8}{13 \times 4.9}$ or $\frac{48.8}{13 \times 4.9} \times 100$ or 76.6[]
(b)	128	4	Using fractions (percentages / decimals): M1 for $\frac{3}{4} \times \frac{3}{8} = \frac{9}{32}$ or $\frac{75}{100} \times 37.5 = 28.125\%$
			<b>A1</b> for $\frac{9}{32}$ or 28.125[%]
			<b>M1</b> for $36 \div \frac{9}{32}$ oe
			or $36 \times \frac{100}{28.125}$ oe
			Partial percentages
			<b>M1</b> for (Remaining) $\frac{100 \times 36}{37.5}$ [= 96]
			<b>A1</b> for 96
			<b>M1</b> for $96 \div \frac{75}{100}$ oe
			SC1 for 288

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			1	T
2	(a)	119.94[] nfww	3	$\mathbf{M2} \text{ for } \frac{62 \times \sin 122}{\sin 26}$
				or <b>M1</b> for $\frac{AC}{\sin 122} = \frac{62}{\sin 26}$ oe
				SC2 for correct answer from alternative methods
	(b)	109 or 108.7 to 108.8 nfww	4	M2 for $119.9^2 + 55^2 - 2 \times 119.9 \times 55\cos 65$ A1 for $11827[\cdot]$ or $11834$ to $11835[\cdot]$ or M1 for implicit version
	(c)	1970 or 1969 to 1970.4	2	<b>M1</b> for $\frac{1}{2} \times 119.9 \times 62 \times \sin 32$
	(d)	22300 or 22310 to 22320	3	<b>M2</b> for $(their (c) + 0.5 \times 55 \times 119.9 \times sin65) \times 4.5$
				or <b>M1</b> for <i>their</i> (c) + 0.5 × 55 × 119.9 × sin65
3	(a)	9 - 2x, $7 - 2x$ oe	2	B1 for each, accept in any order
	(b)	$\begin{cases} x(9-2x)(7-2x) \\ 4x^3 - 32x^2 + 63x \end{cases}$	M1FT A1	Correct expansion and simplification with no errors
	(c)	24 20	2	B1 for each correct value
	(d)	Correct curve	3	<b>B2FT</b> for 5 correct plots or
				<b>B1FT</b> for 3 or 4 correct plots
	(e)	$0.65 \text{ to } 0.75 \le x \le 2 \text{ oe}$	2	<b>B1</b> for 0.65 to 0.75 seen
	(f) (i)	36 to 37	1	
	(ii)	1.2 to 1.4	1	
4	(a)	48 and 84 66 and 66	2	B1 for each pair
	(b)	540	2	M1 for $3 \times 180$ or $(2 \times 5 - 4) \times 90$ or $5 \times (180 - 360 \div 5)$ oe
	(c)	1620	2	<b>M1</b> for $7 \times 360 - their 540 - 360$
	(d) (i)	$\begin{vmatrix} 2x+5+3y-20+4x-5+x+y-10 & = 360 & \text{oe} \end{vmatrix}$	1	Allow partial simplification but not $7x + 4y - 30 = 360$
	(ii)	2x + 5 + 3y - 20 = 180	1	
	(iii)	[x =] 30, [y =] 45 nfww	4	M1 for correct multiplication M1 for correct elimination A1 $x = 30$ or $y = 45$
				If 0 scored <b>SC1</b> for correct substitution to find the other variable
	(iv)	65, 115, 115, 65	1	Accept in any order

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5 (a) (i)	3.81 or 3.812 to 3.813 or 3h 49min nfww	4	M1 for midpoints soi (condone 1 error or omission and M1 for use of $\sum fx$ with $x$ in correct interval including both boundaries (condone 1 further error or omission) and M1 (dep on $2^{\text{nd}}$ M1) for $\sum fx \div 80$ (305 ÷ 80)
(ii)	Correct histogram	4	B1 for each correct block and B1 for correct widths
(b) (i)	$\frac{2}{5}$ , $\frac{1}{4}$ , $\frac{3}{4}$ , $\frac{1}{4}$ oe	2	<b>B1</b> for $\frac{2}{5}$ or both $\frac{1}{4}$ s in correct place
(ii)	$\frac{18}{20}$ nfww $\left[\frac{9}{10}\right]$	3	M2 FT for $1 - their \frac{2}{5} \times their \frac{1}{4}$ or $\frac{3}{5} \times \frac{3}{4} + \frac{3}{5} \times their \frac{1}{4} + their \frac{2}{5} \times \frac{3}{4}$ oe or  M1 FT for $their \frac{2}{5} \times their \frac{1}{4}$ or $\frac{3}{5} \times their \frac{1}{4} + their \frac{2}{5} \times \frac{3}{4}$ oe
(iii)	$\frac{27}{125}$ [0.216]	2	<b>M1</b> for $\frac{3}{5} \times \frac{3}{5} \times \frac{3}{5}$
6 (a) (b)	329.7 to 330 2970 or 2967 to 2969.[]	3	M2 for $\frac{1}{2}\pi(12^2 + 8.75^2 - 3.25^2)$ oe or M1 for $\frac{1}{2}\pi12^2$ or $\frac{1}{2}\pi8.75^2$ or $\frac{1}{2}\pi3.25^2$ SC2 for answer 1318 to 1320 M3 for $\frac{1}{2}\pi(24 + 17.5 + 6.5) \times 35 + their$ (a)
			or M2 for $\frac{1}{2}\pi(24 + 17.5 + 6.5) \times 35$ or M1 for $\frac{1}{2}\pi \times 24$ or $\frac{1}{2}\pi \times 17.5$ or $\frac{1}{2}\pi \times 6.5$ SC3 for 3955 to 3960 dep on SC2 in (a)
(c)	11.5 or 11.6 or 11.53 to 11.55	3FT	M1 for their (a) × 35 A1 for 11500 or 11530 to 11550

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(d) (i)	$\frac{r}{h} = \frac{20}{40}$ or $\frac{r}{20} = \frac{h}{40}$	1	Accept 20: 40 = $r$ : $h$ leading to $40r = 20h$ [ $r = h/2$ ] $\frac{20}{40} = \frac{1}{2} \text{ and } \frac{r}{h} = \frac{1}{2}$
(ii)	35.3 or 35.31 to 35.34	3	M2 for $\sqrt[3]{\frac{their  11545 \times 12}{\pi}}$ oe or $2 \times their  r$
			<b>M1</b> for their 11545 = $\frac{1}{3} \times \pi \times \left(\frac{h}{2}\right)^2 \times h$ oe
			or their 11545 = $\frac{1}{3} \times \pi \times r^2 \times 2r$ oe
7 (a) (i)	$\frac{3}{2}$ or 1.5	2	<b>M1</b> for $\frac{14 - (-4)}{8 - (-4)}$ oe
(ii)	$y = \frac{3}{2}x + 2 \text{ oe}$	2	<b>B1</b> for $y = their \frac{3}{2}x + c$ o.e. or $y = mx + 2$ , $m \neq 0$
			SC1 for $\frac{3}{2}x+2$
(iii)	$\begin{pmatrix} 12 \\ 18 \end{pmatrix}$	1	
(iv)	21.6 or 21.63[]	2	<b>M1 FT</b> for their $12^2$ + their $18^2$ oe
(b) (i)	(a) $3b - 4a$	1	
	<b>(b)</b> $\frac{1}{5}(6\mathbf{b} - 8\mathbf{a})$ oe simplified	2	<b>M1</b> for $\frac{1}{5}(12\mathbf{a} + 6\mathbf{b}) - 4\mathbf{a}$ or $AR = AO + OR$
	(c) $6\mathbf{a} + 3\mathbf{b}$ oe simplified	1	
(ii)	OR is parallel to OT	1	Dep on $\overrightarrow{OT}$ correct
(iii)	$\frac{9}{4}$ or 2.25	2	M1 for $\left(\frac{3}{2}\right)^2$

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8	(a)	$\frac{2(s-ut)}{t^2}$ oe nfww	3	<ul> <li>M1 for a correct rearrangement to isolate the a term and</li> <li>M1 for a correct multiplication by 2 and</li> <li>M1 for a correct division by t²</li> </ul>
	(b)	36.75 cao	3	M2 for 15.5 + 2.5 × 8.5 B1 for two of 15.5, 2.5, 8.5 seen
	(c) (i)	$\frac{16}{5}$ or better [3.2]	1	
	(ii)	11.2	4	M2 for $\frac{1}{2}(25 + 10)16$ (= 280) or M1 for appreciation of distance from area and M1 for <i>their</i> 280 ÷ 25 (dep on M1)
9	(a)	15 18 $3n+3$ or $3(n+1)$ 6 10 25 36 $(n+1)^2$	9	B2 for 15, 6, 25 or B1 for two correct values  B3 for 18, 10, 36 or B1 for each correct value  B2 for $3n + 3$ oe or M1 for $3n + k$ , for any $k$ B2 for $(n + 1)^2$ oe or M1 for a quadratic expression
	(b)	14	2	M1 for $(n+1)(n+2) = 240$ or better or $15 \times 16 = 240$
	(c) (i)	$\frac{1}{2} + p + q = 9$	1	
	(ii)	$[p=] 3$ $[q=] \frac{11}{2}$	5	<b>B2</b> for $4p + 2q = 23$ or <b>B1</b> for $\frac{1}{2} \times 2^3 + p \times 2^2 + q \times 2$ oe <b>M1</b> for correct multiplication and subtraction of <i>their</i> equations <b>A1</b> for $[p = ]$ 3 or $[q = ]$ $\frac{11}{2}$ If 0 scored then <b>SC1</b> for either correct

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10 (a)	$\frac{x}{x+3}$ cao	3	<b>B1</b> for $(x+3)(x-3)$ <b>B1</b> for $x(x-3)$
(b)	$\frac{3}{2}$ and $-5$	7	M2 for $15(x+1) - 20x = 2x(x+1)$ or M1 for multiplication by one denominator only or $\frac{15(x+1) - 20x}{x(x+1)}$ and B2 for $2x^2 + 7x - 15$ [= 0] or B1 for $15x + 15 - 20x$ or $2x^2 + 2x$ and M2 for $(2x-3)(x+5)$ or <i>their</i> correct factors or formula or M1 for $(2x+a)(x+b)$ where $ab = -15$ or $a + 2b = 7$ A1 for $x = \frac{3}{2}$ and $-5$